# Probing the See Saw Mechanism at Future Hadron Colliders 

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My pronouns: he/him/his
1812.01630: J.C. Helo, H. Li, N. Neill, MJRM, J.C. Vasquez
1810.09450: Y. Du, A. Dunbrack, MJRM, J.-H. Yu 1806.08499: B. Dev, MJRM, Y. Zhang

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## Goals For This Talk

- Illustrate how studies of the tri-lepton channel at the HL/HE-LHC \& a 100 TeV pp collider may help distinguish between mLRSM and non-minimal LRSM/minimal types I or II see saw mechanisms
- Illustrate reach of a 100 TeV collider for discovery and characterization of type II see saw scalar sector
- Encourage future work


## Outline

I. ContextII. Type I+II See Saw \& LRSMIII. Tri-lepton Channel at pp Colliders
IV. Probing the Scalar PotentialV. Outlook

## I. Context

## Neutrino Mass Low-Energy EFT

$$
\mathcal{L}_{\text {mass }}=y \bar{L} \tilde{H} \nu_{R}+\text { h.c. } \quad \mathcal{L}_{\text {mass }}=\frac{y}{\Lambda} \bar{L}^{c} H H^{T} L+\text { h.c. }
$$

Dirac
Majorana

## Neutrino Mass Low-Energy EFT

$$
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$$

Dirac
Majorana


#### Abstract

What is the mass scale $\Lambda$ associated with $m_{v}$ generation?


## Neutrino Mass Low-Energy EFT

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$$

Dirac
Majorana

What is the mass scale $\Lambda$ associated with $m_{v}$ generation?


## Neutrino Mass Low-Energy EFT

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\mathcal{L}_{\text {mass }}=y \bar{L} \tilde{H} \nu_{R}+\text { h.c. } \quad \mathcal{L}_{\text {mass }}=\frac{y}{\Lambda} \bar{L}^{c} H H^{T} L+\text { h.c. }
$$

Dirac
Majorana

## What is the mass scale $\Lambda$ associated with $m_{v}$ generation?

What are the corresponding dynamics?


## Neutrino Mass Models

- Type I see-saw
- Type II see-saw
- Type III see-saw
- Inverse see-saw
- Radiative
" $v S M ", ~ " v M S S M "$, LRESM

GUTS
LRSM
MSSM

+ combinations \& many other examples


## Type I See-Saw

$$
\mathcal{L}_{\text {mass }}=y \bar{L} \tilde{H} \nu_{R}+\text { h.c. } \quad \mathcal{L}_{\text {mass }}=\frac{y}{\Lambda} \bar{L}^{c} H H^{T} L+\text { h.c. }
$$

Majorana


Type I: $N_{R} S U(2)_{L}$ singlet
Type III: $N_{R} S U(2)_{L}$ triplet

## Type I See-Saw

$$
\mathcal{L}_{\text {mass }}=y \bar{L} \tilde{H} \nu_{R}+\text { h.c. } \quad \mathcal{L}_{\text {mass }}=\frac{y}{\Lambda} \bar{L}^{c} H H^{T} L+\text { h.c. }
$$

Majorana


Type II: $\Delta_{L} S U(2)_{L}$ triplet

Type I: $N_{R} S U(2)_{L}$ singlet Type III: $N_{R} S U(2)_{L}$ triplet

## Type II See-Saw

$$
\mathcal{L}_{\text {mass }}=y \bar{L} \tilde{H} \nu_{R}+\text { h.c. } \quad \mathcal{L}_{\text {mass }}=\frac{y}{\Lambda} \bar{L}^{c} H H^{T} L+\text { h.c. }
$$

Majorana

Introduce "Complex Triplet": $\Delta_{L} \sim(1,3,2)$

$$
\begin{gathered}
\Delta_{L}=\left(\begin{array}{cc}
\Delta^{+} \sqrt{2} & \Delta^{++} \\
\Delta^{0} & -\Delta^{+} \sqrt{2}
\end{array}\right) \\
\mathcal{L}=\frac{g}{2} h_{i j}\left[\bar{L}^{C_{i}} \varepsilon \Delta_{L} L^{j}\right]+\text { h.c. }
\end{gathered}
$$



$$
\frac{y}{\Lambda} \sim g h\left(\frac{\mu}{m_{\Delta}}\right) \frac{1}{m_{\Delta}}
$$

## See Saw Scenarios

| Model Class | Minimal | LRSM | $\Delta V$ |
| :--- | :---: | :---: | :---: |
| Type I | $\checkmark$ | $\checkmark$ | $*$ |
| Type II | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Type III | $\checkmark$ | $\star$ | $*$ |
| Inverse | $\checkmark$ | $\checkmark$ | $*$ |

## See Saw Scenarios

| Model Class | Minimal | LRSM | $\Delta V$ |
| :--- | :---: | :---: | :---: |
| Type I | $\checkmark$ | $\boxed{ }$ | $*$ |
| Type II | $\checkmark$ | $\checkmark$ | $\searrow$ |
| Type III | $\checkmark$ | $\star$ | $*$ |
| Inverse | $\checkmark$ | $\checkmark$ | $*$ |

This Talk: How can we probe with LHC \& future pp colliders

## Comments

- Many other earlier works on see saw collider pheno (e.g. Keung \& Senjanovic '83, Perez et al '08, Nemevsek et al '12, Han et al '13, Izaguirre \& Shuve ' $15, \cdots$ ) Apologies to others not cited here!
- Following assumes see saw scale at the 10's of TeV or below


## II. Types I + II See Saw \& LRSM

## See Saw Scenarios

| ModeI Class | Minimal |  | LRSM | $\Delta V$ |
| :--- | :---: | :---: | :---: | :---: |
| Type I | $\checkmark$ | $\boxed{ }$ | $*$ |  |
| Type II | $\nearrow$ |  | $\checkmark$ | $\checkmark$ |
| Type III | $\checkmark$ | $*$ | $*$ |  |
| Inverse | $\checkmark$ | $\checkmark$ | $*$ |  |

How to distinguish minimal LRSM from nonminimal LRSM or other minimal scenarios

## Minimal Left-Right Symmetric Model

Two sources of $m_{v}$ :

$$
\begin{gathered}
\mathcal{L}=\frac{g}{2} h_{i j}\left[\bar{L}^{C_{i}} \varepsilon \Delta_{L} L^{j}\right]+(L \leftrightarrow R)+\text { h.c. + Yukawa } \\
\mathcal{L}_{\text {mass }}=\left(\begin{array}{ll}
\bar{\nu}_{L} & \bar{N}_{R}^{C}
\end{array}\right)\left(\begin{array}{cc}
0 & m_{D} \\
m_{D} & M_{N}
\end{array}\right)\binom{\nu_{L}}{N_{R}}+m_{L} \bar{\nu}_{L}^{C} \nu_{L}
\end{gathered}
$$

## Minimal Left-Right Symmetric Model

Two sources of $m_{v}$ :

$$
\mathcal{L}=\frac{g}{2} h_{i j}\left[\bar{L}^{C_{i}} \varepsilon \Delta_{L} L^{j}\right]+(L \leftrightarrow R)+\text { h.c. + Yukawa }
$$

Type I see-saw
Type II see-saw


$$
m_{N} \sim g h_{R}\left\langle\Delta_{R}^{0}\right\rangle
$$

$m_{L} \sim g h_{L}\left\langle\Delta_{L}^{0}\right\rangle$

## Non-Minimal Left-Right Symmetric Model

LRSM inverse see saw:
Add gauge singlet neutral leptons
w/ Majorana mass $\mu$

$$
\begin{aligned}
& \mathcal{M}=\left(\begin{array}{ccc}
0 & M_{D}^{T} & 0 \\
M_{D} & 0 & M_{N} \\
0 & M_{N}^{T} & \mu
\end{array}\right) \\
& M_{\nu} \simeq M_{D}^{T} \frac{1}{M_{N}^{T}} \mu \frac{1}{M_{N}} M_{D}
\end{aligned}
$$

## Heavy-Light Neutrino Mixing

Mass matrix diagonalization

$$
\begin{gathered}
\binom{\nu^{\prime}}{N^{\prime c}}=\left(\begin{array}{cc}
1 & \Theta \\
-\Theta^{T} & 1
\end{array}\right)\binom{\nu}{N^{c}} \\
\Theta \simeq M_{D}^{*} M_{N}^{-1}
\end{gathered}
$$

## Heavy-Light Neutrino Mixing

Mass matrix diagonalization

$$
\binom{\nu^{\prime}}{N^{\prime c}}=\left(\begin{array}{cc}
1 & \Theta \\
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\end{array}\right)\binom{\nu}{N^{c}}
$$

$$
\Theta \simeq M_{D}^{*} M_{N}^{-1}
$$

Colliders:
Probe $\Theta$ for $M_{N}$ at or below O(few) TeV

Models:

- Minimal LRSM: predict $\Theta$
- Minimal type I or nonminimal LRSM: $\Theta$ arbitrary


## Heavy-Light Neutrino Mixing

Minimal Model

$$
M_{D}=V_{L}^{*} \hat{M}_{N} \sqrt{\frac{v_{L}}{v_{R}}-\frac{\hat{M}_{\nu}}{\hat{M}_{N}}} V_{L}^{\dagger}
$$

Non-Minimal Model

$$
V_{R}^{\dagger} M_{D}=\hat{M}_{N} U_{R}^{\dagger} \frac{1}{\sqrt{\hat{\mu}}} \mathcal{R} \sqrt{m_{\nu}} V_{L}^{\dagger}
$$

## Heavy-Light Neutrino Mixing

Minimal Model


Non-Minimal Model


## Heavy-Light Neutrino Mixing

Minimal Model


Non-Minimal Model
Arbitrary (Casas-Ibarra)


## III. Tri-Lepton Channel at pp Colliders

1812.01630: J.C. Helo, H. Li, N. Neill, MJRM, J.C. Vasquez

## Tri-Lepton Channel



- Relatively clean
- Previous work min type I
- Study prompt decay region
- Analysis: back up slides


## Tri-Lepton Channel



- Relatively clean
- Previous work min type I
- Study prompt decay region
- Analysis: back up slides

Dominant: $N_{1} \rightarrow W_{R}{ }^{*} l \rightarrow j j \mid$

$$
\begin{aligned}
& \Gamma\left(N \rightarrow l^{ \pm} l^{\prime \mp} \nu\right)=\left(\left|\left(\Theta_{L}\right)_{l N}\right|^{2}+\left|\left(\Theta_{L}\right)_{l^{\prime} N}\right|^{2}\right) \\
& \quad x \frac{G_{F}^{2}}{96 \pi^{4} m_{N}} \int_{0}^{m_{N}^{2}} d x \frac{\pi\left(m_{N}^{2}-x\right)\left(m_{N}^{4}+x m_{N}^{2}-2 x^{2}\right)}{m_{N}^{2}\left(1-\frac{x}{M_{W}^{2}}\right)^{2}}
\end{aligned}
$$

$m L R S M N_{1} B R$


## Sensitivities

LHC $3 a b^{-1}$





## Sensitivities



## Sensitivities





- Observation of the tri-lepton channel at the HL/HE-LHC $\rightarrow$ non-minimal model or minimal type I
- Observing the tri-lepton channel in the mLRSM $\rightarrow$ 100 TeV pp collider needed


## Interpreting a Signal

100 TeV pp


Probing $\mathrm{O}(\mathrm{MeV})$ Dirac masses

## IV. Probing the Scalar Potential

1810.09450: Y. Du, A. Dunbrack, MJRM, J.-H. Yu

- If tri-lepton signal seen at HL/HE-LHC how distinguish between minimal type I, minimal type II, or non-minimal LRSM?
- If tri-lepton signal first seen at $100 \mathrm{TeV} p p$ collider, how confirm it is in context of $L R$ symmetry


## See Saw Scenarios

| Model Class | Minimal | LRSM | $\Delta V$ |
| :--- | :---: | :---: | :---: |
| Type I | $\checkmark$ | $\checkmark$ | $\star$ |
| Type II | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Type III | $\nearrow$ | $\star$ | $\star$ |
| Inverse | $\nearrow$ | $\nearrow$ | $\star$ |

- Follow on to Perez et al '08
- No assumption of $L R$ symmetry


## Minimal Type II Potential

$$
\begin{aligned}
V(\Phi, \Delta)= & -m^{2} \Phi^{\dagger} \Phi+M^{2} \operatorname{Tr}\left(\Delta^{\dagger} \Delta\right)+\left[\mu \Phi^{\mathrm{T}} \mathrm{i} \tau_{2} \Delta^{\dagger} \Phi+\text { h.c. }\right]+\lambda_{1}\left(\Phi^{\dagger} \Phi\right)^{2} \\
& +\lambda_{2}\left[\operatorname{Tr}\left(\Delta^{\dagger} \Delta\right)\right]^{2}+\lambda_{3} \operatorname{Tr}\left[\Delta^{\dagger} \Delta \Delta^{\dagger} \Delta\right]+\lambda_{4}\left(\Phi^{\dagger} \Phi\right) \operatorname{Tr}\left(\Delta^{\dagger} \Delta\right)+\lambda_{5} \Phi^{\dagger} \Delta \Delta^{\dagger} \Phi
\end{aligned}
$$

## Minimal Type II Potential

$$
\begin{aligned}
V(\Phi, \Delta)= & -m^{2} \Phi^{\dagger} \Phi+M^{2} \operatorname{Tr}\left(\Delta^{\dagger} \Delta\right)+\left[\mu \Phi^{\mathrm{T}} \mathrm{i} \tau_{2} \Delta^{\dagger} \Phi+\text { h.c. }\right]+\lambda_{1}\left(\Phi^{\dagger} \Phi\right)^{2} \\
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\end{aligned}
$$

- How to discover $\Delta$ scalars ?
- How to determine potential parameters ?


## Minimal Type II Potential

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\end{aligned}
$$

- How to discover $\Delta$ scalars?
- How to determine potential parameters ?

| Parameter | Significance | Probe |
| :--- | :--- | :--- |
| $\mu$ | Type II $m_{v}$ | Neutrino mass |
| $\lambda_{5}$ | $\Delta$ mass spectrum | $\Delta$ mass splittings |
| $\lambda_{4}$ | Higgs portal | $H^{+}$decays |
| $\lambda_{2,3}$ | $\Delta$ self interaction | Challenging |

## Discovery

| Production | Decay mode + final state | Regime |
| :--- | :--- | :--- |
| $\mathrm{H}^{++} \mathrm{H}^{-}$ | $I^{+} I^{+} I^{-}$ | Small $v_{\Delta}$ |
| $\mathrm{H}^{++} \mathrm{H}^{++}$ | $W^{+} W^{+} W-W^{-} \rightarrow I^{+} I^{+} I^{-}+M E T$ | Large $v_{\Delta}$ |
| $\mathrm{H}^{++} \mathrm{H}^{-}$ | $I^{+}+h W^{-} \rightarrow I^{++}$bb $I^{-}+\mathrm{MET}$ | Intermediate $v_{\Delta}$ |
| $H^{++} H^{-}$ | $W^{+} W^{+} h W^{-} \rightarrow I^{+} I^{+} b b I^{-}+M E T$ | Intermediate $v_{\Delta}$ |

## Discovery





## Discovery



This study



## Discovery



## Discovery



## Probing the Scalar Potential: $\lambda_{5}$

$$
m_{H^{++}}^{2}-m_{H^{+}}^{2} \simeq-\frac{\lambda_{5}}{4} v_{H}^{2}
$$

## Probing the Scalar Potential

$$
\begin{aligned}
& \Phi=\left[\begin{array}{c}
\varphi^{+} \\
\frac{1}{\sqrt{2}}\left(\varphi+v_{\Phi}+i \chi\right)
\end{array}\right] \quad \Delta=\left[\begin{array}{cc}
\frac{\Delta^{+}}{\sqrt{2}} & H^{++} \\
\frac{1}{\sqrt{2}}\left(\delta+v_{\Delta}+i \eta\right) & -\frac{\Delta^{+}}{\sqrt{2}}
\end{array}\right] \\
& \binom{\varphi}{\delta}=\left(\begin{array}{cc}
\cos \alpha & -\sin \alpha \\
\sin \alpha & \cos \alpha
\end{array}\right)\binom{h}{H}
\end{aligned}
$$

$$
\tan 2 \alpha \approx \frac{v_{\Delta}}{v_{\Phi}} \cdot \frac{2 v_{\Phi}^{2} \lambda_{45}-4 m_{\Delta}^{2}}{2 \lambda_{1} v_{\Phi}^{2}-m_{\Delta}^{2}} \approx \frac{v_{\Delta}}{v_{\Phi}} \cdot \frac{2 v_{\Phi}^{2} \lambda_{45}-4 m_{\Delta}^{2}}{m_{h}^{2}-m_{\Delta}^{2}}
$$

## Probing the Scalar Potential

$$
\begin{aligned}
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\end{array}\right] \\
& \binom{\varphi}{\delta}=\left(\begin{array}{cc}
\cos \alpha-\sin \alpha \\
\sin \alpha & \cos \alpha
\end{array}\right)\binom{h}{H}
\end{aligned}
$$

Triplet mass scale

$$
\tan 2 \alpha \approx \frac{v_{\Delta}}{v_{\Phi}} \cdot \frac{2 v_{\Phi}^{2} \lambda_{45}-4 m_{\Delta}^{2}}{2 \lambda_{1} v_{\Phi}^{2}-m_{\Delta}^{2}} \approx \frac{v_{\Delta}}{v_{\Phi}} \cdot \frac{2 v_{\Phi}^{D_{\Phi}} \lambda_{45}-4 m_{\Delta}^{2}}{m_{h}^{2}-m_{\Delta}^{2}}
$$

## Probing the Scalar Potential



| Vertex | Coupling |
| :---: | :---: |
| $h A Z$ | $-\frac{g}{2 \cos \theta_{W}}\left(\cos \alpha \sin \beta_{0}-2 \sin \alpha \cos \beta_{0}\right)$ |
| $H Z Z$ | $\frac{2 i e m_{Z}}{\sin 2 \theta_{W}}\left(2 \sin \beta_{0} \cos \alpha-\cos \beta_{0} \sin \alpha\right)$ |
| $H W^{+} W^{-}$ | $i g m_{Z} \cos \theta_{W}\left(\sin \beta_{0} \cos \alpha-\cos \beta_{0} \sin \alpha\right)$ |
| $h H^{-} W^{+}$ | $\frac{i g}{2}\left(\sin \beta_{ \pm} \cos \alpha-\sqrt{2} \cos \beta_{ \pm} \sin \alpha\right)$ |

## Probing the Scalar Potential



| Vertex | Coupling |
| :---: | :---: |
| $h A Z$ | $-\frac{g}{2 \cos \theta_{W}}\left(\cos \alpha \sin \beta_{0}-2 \sin \alpha \cos \beta_{0}\right)$ |
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## Probing the Scalar Potential

| Production | Decay mode + final state | Regime |
| :--- | :---: | :--- |
| $H^{++} H^{-}$ | $I^{+} I^{+} h W^{-} \rightarrow I^{+} I^{+} b b I^{-}+M E T$ | Intermediate $v_{\Delta}$ |
| $H^{++} H^{-}$ | $W^{+} W^{+} h W^{-} \rightarrow I^{+} I^{+}$bb $I^{-}+M E T$ | Intermediate $v_{\Delta}$ |


| Vertex | Coupling |
| :---: | :---: |
| $h A Z$ | $-\frac{g}{2 \cos \theta_{W}}\left(\cos \alpha \sin \beta_{0}-2 \sin \alpha \cos \beta_{0}\right)$ |
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| $H W^{+} W^{-}$ | $i g m_{Z} \cos \theta_{W}\left(\sin \beta_{0} \cos \alpha-\cos \beta_{0} \sin \alpha\right)$ |
| $h H^{-} W^{+}$ | $\frac{i g}{2}\left(\sin \beta_{ \pm} \cos \alpha-\sqrt{2} \cos \beta_{ \pm} \sin \alpha\right)$ |

## Probing the Scalar Potential



## Probing the Scalar Potential



## V. Outlook

- Uncovering the origin of $m_{v}$ is a key open problem in particle physics and one for which a variety of experimental probes are needed
- For $m_{v}$ dynamics at the TeV scale or below, hadron colliders could provide unique tests of the see saw mechanism
- The tri-lepton channel can be used to probe the heavylight neutrino mixing angle, and a comparison of HL/HELHC and 100 TeV pp collider searches could distinguish the minimal LRSM scenario from other see saw mechanisms
- A 100 TeV pp collider could significantly extend the discovery reach for scalars associated with the type II scenario and probe a variety of scalar sector couplings
- There exist many opportunities for additional studies हो others are encouraged to get involved!


## Back Up Slides

## Heavy-Light Neutrino Mixing

Minimal Model

$$
\begin{aligned}
\Theta & =\sqrt{\epsilon-M_{N}^{-1} M_{\nu}}=M_{D}^{*} M_{N}^{-1} \quad \Theta_{L}=\Theta V_{R}^{*}, \quad \Theta_{R}=\Theta V_{L}^{*} . \\
M_{D} & =V_{L}^{*} \hat{M}_{N} \sqrt{\frac{v_{L}}{v_{R}}-\frac{\hat{M}_{\nu}}{\hat{M}_{N}}} V_{L}^{\dagger}
\end{aligned}
$$

Non-Minimal Model

$$
\Theta_{L}=\frac{1}{\sqrt{2}} M_{D}^{\dagger} V_{R} \hat{M}_{N}^{-1} \quad V_{R}^{\dagger} M_{D}=\hat{M}_{N} U_{R}^{\dagger} \frac{1}{\sqrt{\hat{\mu}}} \mathcal{R} \sqrt{m_{\nu}} V_{L}^{\dagger}
$$

## Analysis: Backgrounds

## ttZ, ttW, tt (j), WZ (j), 3W, Z/ү (j)

## Cuts

| Cut description |  |
| :---: | :---: |
| $e^{+} e^{+} \mu^{-}$, no $b$ jets and no additional leptons | signal selection |
| $p_{T, e^{+}}^{l e a d}>200 \mathrm{GeV}, p_{T, e^{+}}^{\text {sub }}>100 \mathrm{GeV}, p_{T, \mu^{-}}^{\text {lead }}>100 \mathrm{GeV}$ | reduce all backgrounds |
| $\begin{gathered} \mathbb{F}_{T}>100 \mathrm{GeV} \\ \left.\left\|m_{\text {inv }}\left(e^{+} e^{+}\right)-91.2\right\|\right)>10 \mathrm{GeV} \end{gathered}$ | reduce mostly $t \bar{t}(j)$ and $Z / \gamma(j)$ reduce mostly $W Z(j)$ |
| $m_{T}\left(e_{s u b}^{+} E_{T}\right)<150 \mathrm{GeV}$ | select channel shown in Fig. 1 (right) |
| $m_{T}\left(e^{+} e^{+} \mu^{-} \mathbb{E}_{T}\right)>M_{W_{R}} / 2$ | reduce all backgrounds |

## Analysis: Cuts

## 100 TeV pp

| Cut description |  |
| ---: | :---: |
| $e^{+} e^{+} \mu^{-}$, no $b$ jets and no additional leptons | signal selection |
| $p_{T, e^{+}}^{\text {lead }}>200 \mathrm{GeV}, p_{T, e^{+}}^{\text {sub }}>100 \mathrm{GeV}, p_{T, \mu^{-}}^{l e a d}>100 \mathrm{GeV}$ | reduce all backgrounds |
| $\mathbb{E}_{T}>100 \mathrm{GeV}$ | reduce mostly $t \bar{t}(j)$ and $Z / \gamma(j)$ |
| $\left.\left\|m_{\text {inv }}\left(e^{+} e^{+}\right)-91.2\right\|\right)>10 \mathrm{GeV}$ | reduce mostly $W Z(j)$ |
| $m_{T}\left(e_{\text {sub }}^{+} \mathbb{E}_{T}\right)<150 \mathrm{GeV}$ | select channel shown in Fig. 1 (right) |
| $m_{T}\left(e^{+} e^{+} \mu^{-} \mathbb{E}_{T}\right)>M_{W_{R}} / 2$ | reduce all backgrounds |



## Analysis: Cuts

## 100 TeV pp

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| $m_{T}\left(e^{+} e^{++} \mu^{-} \mathbb{E}_{T}\right)>M_{W_{R}} / 2$ | reduce all backgrounds |



## Analysis: Cuts

|  | Backgrounds |  |  |  |  |  | Signal |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sqrt{s}=13 \mathrm{TeV}$ | $t \bar{t} Z$ | $t \bar{t} W$ | $t \bar{t}(j)$ | $W Z(j)$ | $3 W$ | $Z / \gamma(j)$ | $m_{N}(100 \mathrm{GeV}) m_{N}(500 \mathrm{GeV})$ |  |
| $e^{+} e^{+} \mu^{-}(\mathrm{b}-$-veto $)$ | 11.8 | 74.9 | 23058 | 24.8 | 6.71 | 901 | 1293 | 371 |
| $P_{T}$ cuts | 0.325 | 3.75 | 216 | 0.215 | 2.33 | 5.31 | 825 | 253 |
| $\mathbb{E}_{T} \mathrm{GeV}$ | 0.158 | 1.85 | 117 | 0.0761 | 1.06 | 0.0911 | 646 | 188 |
| $m_{\text {inv }}\left(e^{+} e^{+}\right)$ | 0.155 | 1.82 | 113 | 0.0761 | 1.05 | 0 | 646 | 188 |
| $m_{T}\left(e_{\text {sub }}^{+} E_{T}\right)$ | 0.0582 | 0.743 | 48.4 | 0.0277 | 0.491 | 0 | 622 | 176 |
| $m_{T}\left(e^{+} e^{+} \mu^{-} \mathbb{E}_{T}\right)$ | 0 | $7.82 \times 10^{-3}$ | 0 | 0 | 0.0169 | 0 | 597 | 158 |




## Analysis: Efficiencies

$$
r \equiv \frac{\operatorname{Br}\left(N_{1} \rightarrow e^{+}\left(W^{-} \rightarrow \mu^{-} \overline{\nu_{\mu}}\right)\right)}{\operatorname{Br}\left(N_{1} \rightarrow \mu^{-}\left(W^{+} \rightarrow e^{+} \nu_{e}\right)\right)}
$$

$M_{\mathrm{kg}}=2 \mathrm{TeV}, \mathrm{M}_{\mathrm{N} 3}=2.5 \mathrm{TeV}, \mathrm{FCC}$

$M_{v e}=2 \mathrm{TeV}, M_{v 3}=2.5 \mathrm{TeV}, \mathrm{FCC}$


